Abstract

Reliable construction waste generation data is a prerequisite for any evidence-based waste management effort, but such data remains scarce in many developing economies owing to their rudimentary recording systems. By referring to several models proposed for estimating waste generation, this study aims to develop a reliable and accessible method for estimating construction waste generation based on limited publicly available data. The study has two objectives. Firstly, it aims to estimate construction waste generation by focusing on the Greater Bay Area (GBA) in China, one of the world’s most thriving regions in terms of construction activities. Secondly, it aims to compare the strengths and weaknesses of various waste quantification models. 43 sets of annual socio-economic, construction-related and C&D waste generation data ranging from 2005 to 2019 were collected from the local government authorities. By analyzing the data using four types of machine learning models, namely multiple linear regression, decision tree, grey models, and artificial neural network, it is found that all calibrated models, with their respective strengths and weaknesses, can produce acceptable results with the testing $R^2$ ranging from 0.756 to 0.977. This study also reveals that the 11 cities in the GBA produced a total of about 364 million m$^3$ of construction waste in 2018. The result can be used for monitoring the urban metabolism, quantifying carbon emission, developing a circular economy, valorizing recycled materials, and strategic planning of waste management facilities in the GBA. The research findings also contribute to the methodologies for estimating waste generation using limited data.

Keywords: Construction waste; waste quantification; Greater Bay Area, China; machine learning.

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List of abbreviations:
ANN = artificial neural network
BIM = building information modeling
CART = classification and regression tree
C&D = construction and demolition
CO = total construction output
CP = construction productivity
CSA = classification system accumulation
CWDCS = construction waste disposal charging scheme
CWM = construction waste management
DT = decision tree
dS = development stages of an economy
FC = floor space completed
FCO = floor space under construction
FD = floor space of demolition
FM = factor modeling
FS = floor space of newly started buildings
GBA = greater Bay Area
GC = GDP per capita
GDP = gross domestic product
GM = grey models
GMC = grey model with convolution integral
GRA = grey relational analysis
GRC = generation rate calculation
KMO = Kaiser-Meyer-Olkin
LA = lifetime analysis
ML = machine learning
MLR = multiple linear regression
MSW = municipal solid waste
PCA = principal component analysis
PO = population
$R^2$ = coefficient of determination
SD = standard deviation
SV = site visit
VIF = variance inflation factor
1. Introduction

Construction waste, a term often used interchangeably with construction and demolition (C&D) waste, is the solid waste generated by construction, renovation, or demolition activities (HKEPD, 2015; USEPA, 2016). It comprises inert and non-inert materials including concrete, steel, slurry, wood, glass, etc. C&D waste contributes significantly to environmental degradation (Coelho & De Brito, 2012; Wang et al., 2010), consumes valuable landfill space (Poon et al., 2004), causes geologic hazards and other undesirable consequences (Lu, 2019; Perlez, 2016). Therefore, it needs to be carefully managed.

Information about waste generation is a prerequisite for many waste management strategies, including planning landfill space, determining levies for polluters or subsidies for recyclers, and scheduling companies’ waste management policies. Since what cannot be measured cannot be improved, estimation of waste generation at both regional and project levels has begun to receive worldwide research attention. Wu et al. (2014), for instance, have reviewed 57 studies in C&D waste quantification. Examples of regional studies include Cochran et al. (2007) exploring the accounting, generation, and composition of building-related C&D waste in Florida, and Lu et al. (2017) who estimate that approximately 1.13 billion tons of C&D materials were generated in China during 2014. This paper also has a regional focus.

For regions where waste generation data is regularly collected and released by official recording systems, estimation is unnecessary (Lu et al., 2017). However, emerging regions often do not have such systems in place. There are a plethora of studies on solid waste quantification in the absence of direct data, where other statistics or signs such as population, economic growth, construction expenditure, urban decay, and waste recycling levels, are analyzed to inform waste generation. Such studies often adopt complicated algorithms to estimate waste generation, but may exhibit overfitting where models report closely or exactly fitting results in training datasets but poor results in testing datasets. In addition, few studies have gone beyond the factors that can predict C&D waste generation to understand how much each factor contributes to the prediction.

This study has two purposes. Firstly, it is to estimate construction waste generation in the Greater Bay Area (GBA) of South China. The GBA is chosen for several reasons. It is among China’s most economically active areas, and one in which intense construction activity exists in conflict with the severe environmental degradation it causes. The GBA comprises 11 regions including Hong Kong and Macau (both under the “one country, two systems” constitutional framework), Shenzhen, Guangzhou, and others. Among these 11 regions, economic development is imbalanced and recording systems vary in reliability. The second purpose of our study is to compare the strengths and weaknesses of waste estimation algorithms in terms of accuracy, scalability, and explanatory clarity, and also consider overfitting issues.
2. Estimating solid waste generation

The amount of construction waste generated can be affected by an ocean of factors. Table 1 summarizes the factors that have been used to predict C&D waste generation at a regional level. These factors are of two types: socio-economic or construction-related. Socio-economic factors include gross domestic product (GDP), GDP per capita, population, and others acting as indicators of socio-economic development and providing the context for construction industry development. It has been proven that C&D waste generation ascends in parallel with population expansion, urbanization, and economic development (Kofoworola & Gheewala, 2009; Zhao et al., 2011). Construction-related factors include total construction output, floor space of newly started buildings, floor space completed, and so on (see Table 1). Although it is impossible to obtain the direct amount of C&D waste generation, these factors with reasonable data availability and proper analytics can yield a satisfactory estimate of C&D waste generation.

### Table 1 Factors impacting construction waste generation

<table>
<thead>
<tr>
<th>Reference</th>
<th>Level</th>
<th>Socio-economic factors</th>
<th>Construction-related factors</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hsiao et al. (2002)</td>
<td>City</td>
<td>-</td>
<td>FS, FD</td>
</tr>
<tr>
<td>Kofoworola and Gheewala (2009)</td>
<td>Country</td>
<td>PO</td>
<td>FS, FCO</td>
</tr>
<tr>
<td>Zhao et al. (2011)</td>
<td>City</td>
<td>PO, GDP</td>
<td>FCO, FD</td>
</tr>
<tr>
<td>Song et al. (2015)</td>
<td>City</td>
<td>-</td>
<td>FC</td>
</tr>
<tr>
<td>Tam and Lu (2016)</td>
<td>Country</td>
<td>GDP, GC, DS</td>
<td>CO, CP, FS</td>
</tr>
<tr>
<td>Lu et al. (2017)</td>
<td>Country</td>
<td>GDP</td>
<td>CO, FCO, FC</td>
</tr>
<tr>
<td>Song et al. (2017)</td>
<td>Country</td>
<td>-</td>
<td>FC</td>
</tr>
</tbody>
</table>

Note:
1. Socio-economic factors: DS – development stages of an economy; GC – GDP per capita; PO – population
2. Construction-related factors: CO – total construction output; CP – construction productivity; FC – floor space completed; FCO – floor space under construction; FD – floor space of demolition; FS – floor space of newly started buildings

With the potential factors known, numerous methods have been proposed for estimating construction waste generation. Wu et al. (2014) categorize these methods into six types: site visit (SV), generation rate calculation (GRC), lifetime analysis (LA), classification system accumulation (CSA), factor modeling (FM), and others (e.g., BIM-based automated estimation). The SV method requires the investigator to conduct surveys on site, including direct measurement by surveying the weight or volume (Hoang et al., 2020; Lau et al., 2008) and indirect measurement by adopting other easily accessible indicators, such as hauling tickets (Bakchan & Faust, 2019). For GRC method, the total waste volume can be calculated through multiplying the quantity of a specific unit by its corresponding generation rate, e.g., area-based calculation (Domingo & Batty, 2021; Hoang et al., 2021). The LA method assumes that all buildings must be dismantled after a certain period of lifetime and the C&D waste can be deduced from calculating the sum of the mass to be removed at expiration.
In this study, estimating waste generation in the GBA is a problem at a regional level. Previous studies have engaged FM methods, particularly in MSW or WEEE. This study therefore will deploy FM methods as well while keeping an eye on other methods as reviewed above. Table 2 provides a detailed analysis of previous studies examining locations, levels, methods, models, data, and estimate performance. It can be seen that the machine learning (ML) models, such as multiple linear regression (MLR), grey model (GM), artificial neural network (ANN), and decision tree (DT), are among the most frequently adopted FM methods. ML is a computer program that “optimize a performance criterion using example data or past experience” (Alpaydin, 2020). The ability to automatically learn from data and adapt to changes is the key to ML applications. ML algorithms may not learn everything from data, but can still identify some patterns or regularities which are presented to humans, either explicitly or implicitly. The ML models or algorithms as shown in Table 2, including the type and size of data and model performance, provide very useful references for this study.
Table 2: Machine learning models used to estimate the solid waste generation at a regional level

<table>
<thead>
<tr>
<th>Method</th>
<th>Model</th>
<th>Waste Type</th>
<th>Region</th>
<th>Region level</th>
<th>Type of data</th>
<th>No. of data</th>
<th>Level of data collection</th>
<th>Model input</th>
<th>Model perform. ($R^2$)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear regression</td>
<td>MLR</td>
<td>MSW</td>
<td>Nigeria</td>
<td>Country</td>
<td>Panel data (Monthly)</td>
<td>166</td>
<td>Household</td>
<td>Household income, household size, educational background, social status, occupation, and season of the year</td>
<td>0.88</td>
<td>Afon and Okewole (2007)</td>
</tr>
<tr>
<td>MLR</td>
<td>MSW</td>
<td>Nigeria</td>
<td>Country</td>
<td>Panel data</td>
<td>181</td>
<td>Household</td>
<td>Education, income per household, and number of residents</td>
<td>0.51</td>
<td>Benitez et al. (2008)</td>
<td></td>
</tr>
<tr>
<td>MLR</td>
<td>MSW</td>
<td>Iraq</td>
<td>City</td>
<td>Cross-sectional data</td>
<td>150</td>
<td>Household</td>
<td>Hotel size, expenditure, area and number of staffs</td>
<td>0.80</td>
<td>Abdulredha et al. (2018)</td>
<td></td>
</tr>
<tr>
<td>MLR</td>
<td>MSW</td>
<td>China</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>10</td>
<td>City</td>
<td>Population, total consumption expenditure</td>
<td>0.94</td>
<td>Yuan et al. (2012)</td>
<td></td>
</tr>
<tr>
<td>MLR</td>
<td>MSW</td>
<td>Vietnam</td>
<td>City</td>
<td>Cross-sectional data</td>
<td>100</td>
<td>City</td>
<td>Household size and household income</td>
<td>0.36</td>
<td>Thanh et al. (2010)</td>
<td></td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1)</td>
<td>MSW</td>
<td>Europe</td>
<td>Country level, City level</td>
<td>Panel data (Yearly)</td>
<td>86</td>
<td>Country level, City level</td>
<td>GDP, population, infant mortality rate, household size, life expectancy at birth</td>
<td>0.65</td>
<td>Beigl et al. (2004)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GMC(1,n), NBGMC(1,n)</td>
<td>WEEE</td>
<td>China</td>
<td>Country</td>
<td>Panel data (Yearly)</td>
<td>13</td>
<td>Country</td>
<td>Quantity of household appliances</td>
<td>-</td>
<td>Zhao et al. (2016)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GM(1,1)-n, GM (1, n) and GMC (1, n))</td>
<td>WEEE</td>
<td>USA</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>13</td>
<td>City</td>
<td>Population Density, Household income</td>
<td>0.99</td>
<td>Duman et al. (2019)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GIM(1), GPPM(1) and GLPM(1)</td>
<td>WEEE</td>
<td>Thailand</td>
<td>Country</td>
<td>Panel data (Yearly)</td>
<td>13</td>
<td>Country</td>
<td>Household expenditure, household size, employment, population density, and urbanization</td>
<td>-</td>
<td>Intharathirat et al. (2015)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GM(1,n)</td>
<td>WEEE</td>
<td>China</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>14</td>
<td>City</td>
<td>GDP, population, size, total retail sales, consumption of gas, water and electricity, personal salary</td>
<td>0.98</td>
<td>Liu and Yu (2007)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GM(1,n)</td>
<td>WEEE</td>
<td>China</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>10</td>
<td>City</td>
<td>GDP, population, household expenditure, total sales of consumer goods</td>
<td>0.95</td>
<td>Wang et al. (2012)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GM(1,n)</td>
<td>WEEE</td>
<td>China</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>9</td>
<td>City</td>
<td>GDP, population, retail sales, consumer spending</td>
<td>0.68</td>
<td>Zhang (2013)</td>
</tr>
<tr>
<td>Grey model</td>
<td>GM(1,1), GM(1,n)</td>
<td>WEEE</td>
<td>China</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>9</td>
<td>City</td>
<td>GDP, population, household expenditure, total sales of consumer goods</td>
<td>0.95</td>
<td>Zhang (2013)</td>
</tr>
<tr>
<td>Neural network</td>
<td>ANN, ANFIS, DWT-ANN, DWT-ANFIS, GA-ANN, GA-ANFIS</td>
<td>MSW</td>
<td>India</td>
<td>City</td>
<td>Panel data (Yearly)</td>
<td>19</td>
<td>City</td>
<td>Previous waste generation</td>
<td>0.87</td>
<td>Soni et al. (2019)</td>
</tr>
<tr>
<td>Neural network</td>
<td>ANN, GM(1,1), MLR</td>
<td>MSW</td>
<td>China</td>
<td>Country</td>
<td>Panel data (Yearly)</td>
<td>16</td>
<td>Country</td>
<td>GDP, population, urbanization, energy consumption</td>
<td>0.93</td>
<td>Chhay et al. (2018)</td>
</tr>
<tr>
<td>Neural network</td>
<td>ANN, SVM, ANFIS, kNN</td>
<td>MSW</td>
<td>Australia</td>
<td>City</td>
<td>Panel data (Monthly)</td>
<td>216</td>
<td>City</td>
<td>Previous waste generation</td>
<td>0.98</td>
<td>Abbasi and El Hanandeh (2016)</td>
</tr>
<tr>
<td>Neural network</td>
<td>ANN, ANFIS, SVM, LSSVM, FSVM, MLR</td>
<td>MSW</td>
<td>Iran</td>
<td>City</td>
<td>Cross-sectional data</td>
<td>105</td>
<td>Household</td>
<td>Hospital’s wards, staff, ownership type, inpatients</td>
<td>0.92</td>
<td>Golbraz et al. (2019)</td>
</tr>
<tr>
<td>Method</td>
<td>Model(s)</td>
<td>Country</td>
<td>Waste Type</td>
<td>Data Type</td>
<td>Period</td>
<td>City/County Data</td>
<td>R²</td>
<td>Reference</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Decision tree</td>
<td>DT, ANN</td>
<td>MSW</td>
<td>Canada</td>
<td>Cross-sectional data</td>
<td>1553</td>
<td>City</td>
<td>0.72</td>
<td>Kannangara et al. (2018)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Other machine learning methods</td>
<td>DT, SVM, RNN</td>
<td>MSW</td>
<td>Canada</td>
<td>Panel data (Monthly)</td>
<td>60</td>
<td>City</td>
<td>0.72</td>
<td>Meza et al. (2019)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Decision tree</td>
<td>GM-SVR</td>
<td>C&amp;DW</td>
<td>China</td>
<td>Panel data (Yearly)</td>
<td>30</td>
<td>Country</td>
<td>0.99</td>
<td>Song et al. (2017)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>System dynamics model</td>
<td>GBRT</td>
<td>MSW</td>
<td>USA</td>
<td>Panel data (Weekly)</td>
<td>41412</td>
<td>Building</td>
<td>0.87</td>
<td>Kontokosta et al. (2018)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Time series</td>
<td>ARIMA</td>
<td>C&amp;DW</td>
<td>China</td>
<td>Panel data (Yearly)</td>
<td>9</td>
<td>City</td>
<td>0.99</td>
<td>Dyson and Chang (2005)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Note:

1. MSW – municipal solid waste; WEEE – waste electrical and electronic equipment; C&DW – C&D waste
2. Panel data – data refers to multi-dimensional data frequently involving measurements over time; Cross-sectional data – data collected by observing many subjects at the same point of time or without regard to differences in time
3. MLR – Multiple linear regression; GM – Grey model; GMC – Grey model with convolution integral; NBGMC – Nonlinear grey Bernoulli model with convolution integral; GIM – Grey index model; GPPM – Grey parabola power model; GLPM – Grey logarithm power model; ANN – Artificial neural network; ANFIS – Adaptive neuro-fuzzy inference system; DWT – Discrete wavelet theory; GA – Genetic algorithm; SVM – Support vector machine; kNN – k-nearest neighbors; SVR – Support Vector Regression; LSSVM – Least squares support vector regression; FSVM – Fuzzy logic support vector regression; PCA – Principal component analysis; DT – Decision tree; RNN – Recurrent neural network; GBRT – Gradient boosting regression tree; ARIMA – Autoregressive integrated moving average
4. $R^2$ is the best testing performance of all models if there is more than one model in the literature. If $R^2$ wasn't given, it is calculated by the authors according to the prediction results in the literature.
3. The Greater Bay Area

The GBA comprises the two SARs (special administration regions) Hong Kong and Macau and nine municipalities in China’s Guangdong province. In 2019, the GBA occupied a total area of about 56,000 km² and had a GDP of USD 1,679.5 billion (CMAB, 2020). Although it occupies less than 1% of China’s land area, the GBA’s contribution to national GDP is up to 12% (Cheung, 2019), making it one of the most economically vibrant regions in China. To accommodate its economic activities, massive construction activities have been undertaken or are underway to materialize the supporting infrastructure and building in the GBA.

Meanwhile, huge amounts of C&D waste have been produced. For example, Hong Kong generated about 18.12 million tons of construction waste in 2018 (HKEPD, 2019). If not properly managed, such vast quantities of waste are bound to hinder the sustainable development of the GBA and cause harm to the inhabitants. In an extreme case, a construction waste landslide in 2015 in Shenzhen resulted in 73 deaths and ruined over 30 buildings (Perlez, 2016).

Having recognized the importance of proper construction waste management (CWM), some regions in the GBA have deployed response strategies. In 2006, Hong Kong launched its construction waste disposal charging scheme (CWDCS) under which contractors are charged HK$71 to $200 per ton for waste mandatorily disposed of at designated facilities (Bao et al., 2020). Facing increased pressure after the tragedy in 2015 to better manage its construction waste, Shenzhen has closed all landfills so that contractors are forced to reduce, reuse and recycle construction waste (Bao & Lu, 2020). In some exemplar sites, zero waste is pursued (Lu, Bao, et al., 2021). In recognition of the imbalance in demand and supply among GBA regions, construction waste material sharing has been actively explored. In fact, since 2006 Hong Kong has been sending its construction waste materials to Jiangmen through an official channel for land reclamation (Lu et al., 2020). However, such efforts are still too piecemeal and discrete. Integrated policies and measures are being sought, but reliable data is a prerequisite for their formulation. Hong Kong and Macau have a long-established recording system with detailed waste generation data, which enables better CWM practice. For example, Ahmed and Zhang (2021) developed a multi-stage network-based model to reduce the logistics cost for inert waste management and validated it using sufficient data from Hong Kong. However, other GBA regions may only possess broad socio-economic background data and lack accurate waste quantity and distribution (Ma et al., 2020). Nonetheless, based on previous studies (Li et al., 2020), it is possible to estimate construction waste generation by extrapolating from data-rich to data-scarce regions.
4. Research methods

This study adopted a four-step research method, including (i) collecting relevant data, (ii) selecting alternative models, (iii) developing the selected models, and (iv) cross-validation of models.

4.1 Data collection

Factors that impact C&D waste generation were carefully selected from the literature, based on our own knowledge, and also depending on data availability. In the end, selected factors were (1) population (PO), (2) GDP per capita (GC), (3) total construction output (CO), (4) floor space of newly started buildings (FS), and (5) floor space of buildings completed (FC).

Data relating to these five factors (i.e., the model input) was collected from statistical yearbooks of the National Bureau of Statistics of China. C&D waste generation data (i.e., model output) is quite limited compared to MSW data. However, with increasing C&D waste and city management system maturity, local governments have begun to pay more attention to effective C&D waste management. For example, the Guangzhou Bureau of Ecology and Environment started incorporating C&D waste generation data into its annual solid waste management report in 2016, while the Shenzhen Housing and Construction Bureau began to provide C&D waste generation data from 2014. Hong Kong and Macau’s C&D waste generation data has been available from the Hong Kong Environment Protection Department since 2005 and the Macau Environmental Protection Bureau since 2010, respectively.

Shanghai has relatively good waste generation data and although not within the GBA is comparable with Shenzhen in terms of construction and waste management. Therefore, statistics from Shanghai were also collected for this study.

In total, 43 sets of data were collected based on the availability of annual C&D waste generation data, as shown in the Supplementary Materials. Shanghai and Hong Kong measure C&D waste generation by weight (ton), while other cities measure by volume (cubic meter). For a better comparison, the weight unit was aligned to the volume unit by the bulk density of C&D waste. Lu, Yuan, et al. (2021) calculated the bulk density by analyzing 4.9 million truckloads of C&D waste. The results show that the 5% to 95% percentile interval of bulk density ($\rho_{5\%-95\%}$) is [0.266 tons/m$^3$, 0.971 tons/m$^3$], with the mean value ($\bar{\rho}$) of 0.528 tons/m$^3$ and the median value ($\rho_{0.5}$) of 0.476 tons/m$^3$. In this study, the density of C&D waste for conversion took a value of 0.5 tons/m$^3$.

The descriptive statistics of the collected data and the Pearson correlation coefficient between the model inputs and outputs can be found in the Supplementary Materials. The correlation analysis can serve as a preliminary screening of factors for further modeling (Kannangara et al., 2018). The correlations can be considered negligible when the absolute value of the
Pearson correlation coefficient is less than 0.3 (Pallant, 2011). In this study, all such values are above 0.6, demonstrating that these factors can be adopted for modeling. The strength of the correlation is in order of PO, CO, FS, FC, and GC.

### 4.2 Model selection

In view of the strong ability to extract experience from the previous data, four ML models, namely MLR, DT, GM, and ANN were adopted in this study. MLR and DT have strong interpretability, so were selected to provide explanatory results. GM and ANN are good at fitting and GM in particular has been used extensively in small-sample prediction. These two models were chosen to provide accurate predictive results.

### 4.3 Model development

#### 4.3.1 Multiple linear regression (MLR)

The MLR model adopts a linear equation shown as Eq. (1):

\[
Y = B_0 + \sum_{i=1}^{m} B_i x_i
\]

where \(Y\) is the output, i.e., the total C&D waste volume in this study; \(x_i\) is the input factors; \(B_0\) and \(B_i\) are the regression coefficient; \(m\) is the number of data points. The MLR model was built by fitting this linear equation to input data. The logarithmic transformation operation was applied to (i) improve data normality; and (ii) reduce the difference between data in the same dimension. There are of course significant differences in data of different-sized cities. For example, in 2019, C&D waste of Guangzhou is around 50 times that of Macau. When fitting an MLR model, a slight change in the regression coefficient (slope) can lead to large variances in the prediction values for smaller cities. Furthermore, negative predictive values might occur, which is obviously not reasonable. Therefore, this study takes [\(\lg(x_i)\)] as the inputs and [\(\lg(Y)\)] as the output. In this way, the range of data in a specific dimension is reduced, and there are no negative prediction values.

Before MLR modeling, a principal component analysis (PCA) was conducted to (i) identify the principal components for MLR; and (ii) eliminate the multicollinearity between the inputs, which might affect the outcome of MLR (Pallant, 2011). The variance inflation factor (VIF), shown as Eq. (2), can be used to evaluate multicollinearity.

\[
VIF_x = \frac{1}{1 - R^2_x}
\]

where \(R^2_x\) is the coefficient of determination for the input \(X\). A VIF value of less than 10 is acceptable (Abdulredha et al., 2018). In this study, after PCA, the VIF values of all the extracted components were reduced to 1.0, i.e., the perfect VIF value, indicating that the multicollinearity was eliminated and the data was suitable for MLR. Five MLR models (identified by PCA-MLR-\(t\), \(t = 1, 2, \ldots, 5\)) were built based on the first \(t\) component(s). The PCA results can be found in the Supplementary Materials.
4.3.2 Decision tree (DT)

A decision tree has one root node, internal nodes, and leaf nodes (Tayefi et al., 2017). At the root or internal nodes, the division happens where the information gain reaches its maximum, and the purity of data contained in the sub-nodes increases. The data is divided into smaller groups recursively until certain criteria are met. The classification and regression tree (CART) algorithm was used in this study. The stop criterion for division was set by limiting the number of data points at each leaf node. CART is a binary tree built by greedy algorithm. This means the binary division only reaches the local optimum, without considering the best partition for all the nodes (Kannangara et al., 2018). In this case, the results might be local minima. To solve this problem, the CART algorithm was trained repeatedly with different initial training data. Its performance and errors were analyzed comprehensively. Moreover, since CART is prone to overfitting, some trivial branches were removed by post-pruning, increasing the generality of the CART model (Bramer, 2007). In this study, the cases where the minimum number of data points at leaf nodes (minimum leaf size) is 1, 2, 4, 6, 8, 10, respectively, were investigated. These models are identified by DT-$t$ ($t = 1, 2, 4, 6, 8, 10$).

4.3.3 Grey model (GM)

Construction waste volume is interpreted by a great number of factors, requiring the multivariate grey model, $\text{GM}(m,n)$. In $\text{GM}(m,n)$, $m$ denotes the order of differential equations, while $n$ denotes the number of variables, including input variables and output variables (Duman et al., 2019). The first-order GM, $\text{GM}(1,n)$, has been widely used in terms of prediction and proven to bear high accuracy. The grey model with convolution integral, $\text{GMC}(1,n)$, one of the variants of GM, can achieve higher accuracy than $\text{GM}(1,n)$ (Intharathirat et al., 2015). In this study, $\text{GM}(1,n)$ and $\text{GMC}(1,n)$ were used to predict C&D waste generation and are presented as differential equations, Eq. (3) and Eq. (4), respectively:

\[
x^{(0)}_i(k) + a z^{(1)}_i(k) = \sum_{i=2}^{n} b_i x^{(1)}_i(k) \quad \text{(3)}
\]

\[
x^{(0)}_i(k) + a z^{(1)}_i(k) = \sum_{i=2}^{n} b_i x^{(1)}_i(k) + u \quad \text{(4)}
\]

where $a$, $b_i$ and $u$ are model parameters; $x^{(0)}_i(k)$, denotes $k$th element of the sequence of $i$th factors; $z^{(1)}_i(k)$ denotes the $k$th accumulated generating operation (AGO) values of the sequence of $i$th factor; $z^{(1)}_i(k) = 0.5 x^{(1)}_i(k) + 0.5 x^{(1)}_i(k - 1)$; for output factor, $i = 1$, for input factors, $i = 2,3,\ldots,n$.

Before constructing the GM, grey relational analysis (GRA) was carried out to rank the factors according to their grey relational grades. Each input factor was compared with the model output in regard to variation tendency in order to determine the grey relational grade (Hsu & Wang, 2009). According to the ranked factors for GRA, 10 GMs were trained,
including \[GM(1,2) – GM(1,6)\] and \[GMC(1,2) – GMC(1,6)\]. Each \(GM(1,n)\) or \(GMC(1,n)\) considered one model output factor and the first \((n-1)\) input factor(s).

4.3.4 Artificial neural network (ANN)
An ANN consists of three kinds of layers: input, hidden, and output. The neurons of the input layer and output layer are equal to the number of inputs and outputs, respectively. There can be a single hidden layer or multiple hidden layers, and each hidden layer can have multiple neurons, leading to the diversiform ANN architectures.

This study adopts a feed-forward neural network with a single hidden layer. This ANN architecture has been employed frequently and has performed well (Ojha et al., 2017). Given enough neurons in the single hidden layer, this ANN model can handle arbitrarily complex problems (Duka, 2014). In this study, the number of neurons in the hidden layers was taken as 3, 5, 10, 15, 30, and 50, respectively (identified by \(\text{ANN-}t\), \(t = 3, 5, 10, 15, 30, 50\)). The sigmoid transfer function served as the activation function within ANN (Kannangara et al., 2018). The network was trained with the Levenberg-Marquardt backpropagation algorithm (Yu & Wilamowski, 2011). Similar to MLR, to avoid negative prediction values, the logarithm of collected data was taken as the inputs and outputs of the ANN model.

4.4 Cross validation
To validate these models, the data set was randomly divided into a training set and a testing set by the ratio of 80:20 (Azadi & Karimi-Jashni, 2016). Different partitions of a dataset result in different models, and some are quite sensitive to training data (Cunningham et al., 2000). These models might fall into the local minima, meaning the model is not the optimal solution, especially for DT and ANN. Therefore, 50 iterations of random partitions were performed for each model, and each model was trained 50 times. The 50 iterations were averaged for performance evaluation. The coefficients of determination \(R^2\) were used to evaluate the training and testing performance. They can be calculated by Eq. (5):

\[
R^2 = 1 - \frac{\sum_{k=1}^{m} (\hat{Y}_i - Y_i)^2}{\sum_{k=1}^{m} (Y_i - \bar{Y})^2}
\]  

where \(m\) is the number of data points; \(\hat{Y}_i\) is the forecast value of the total C&D waste volume; \(Y_i\) is the actual value of the total C&D waste volume; \(\bar{Y}\) is the average value of \(Y_i\).

5. Analyses, results and findings
5.1 Multiple linear regression (MLR)
The first \(t\) identified components were the inputs of PCA-MLR-\(t\). Accordingly, five models were trained, and their average performance results are shown in Fig. 1. The PCA-MLR-1 only employed Component 1 and obtained the training \(R^2\) of 0.765, meaning that 76.5% of
the variance can be explained by Component 1. As more components were added to the
model, the training performance improved slightly. The testing $R^2$ shows a similar trend to
the training $R^2$. The five components identified by PCA contain 100% information of the data
set. When modeling, ignoring any one of them can result in information loss. That is the
reason for the performance improvement as the number of components increases. The best-
performing model, PCA-MLR-5, has a training $R^2$ of 0.803 and a testing $R^2$ of 0.777.

The error area, i.e., the shaded area in Fig. 1, illustrates the stability of the model
performance. The width of the error area is equal to twice the standard deviation (SD), with
its center at the average value. Models with narrower error areas can deliver more reliable
results. In Fig. 1, the widths of the testing error area are near twice those of the training error
area. The widths of error areas change not too much for different MLR models, which
demonstrates these MLR models have almost the same stability.

Fig. 1 Average training and testing performance of MLR models

The PCA-MLR-5 model was trained 50 times based on different data partitioning. Among
these models, the one with the closest training and testing $R^2$ to the average $R^2$ occurred in the
17th trial. This model has a training $R^2$ of 0.791 and a testing $R^2$ of 0.787, shown as Eq. (6):

$$Y = 3.510 + 0.028 \times PO - 0.176 \times GC + 0.434 \times CO + 0.079 \times FS - 0.050 \times FC \quad (6)$$
It is worth noting that the model inputs have been normalized to have the same average and variance values, so that the regression coefficients in this model are comparable. It is found that CO has the most significant positive influence, which may be due to the fact that CO directly reflects the level of construction activity. GC has a negative impact on C&D waste generation. In general, high GC means good living conditions for people, sound infrastructural facilities, and high levels of government management. Therefore, GC may contain information about the management level of C&D waste. A higher management level of C&D waste may result in less waste generation. PO, FS, and FC have relatively small coefficients. The regression coefficient of FC is negative, which is probably because the annual FC data fluctuate greatly for some cities.

5.2 Decision Tree (DT)

The complexity of DT was controlled by the minimum leaf size. In general, the bigger the leaf size, the simpler the model. The results under different minimum leaf sizes are presented in Fig. 2(a). The training $R^2$ decreases as the minimum leaf size increases, while the testing $R^2$ rises slightly first and then goes down significantly. The decrease in training $R^2$ is because the DT model becomes so simple that it is not able to accurately define the rules existing in the data. The variations of testing $R^2$ are closely related to the overfitting and underfitting problems. When the minimum leaf size is small, the model is too complicated to generalize the trained model to the testing data, and the problem is overfitting. When the minimum leaf size is too large, the model is simple and not fully developed, and the problem is underfitting. The optimal model is DT-2, i.e., with a minimum leaf size of 2. Its training and testing $R^2$ are 0.853 and 0.756, respectively. When the model is simple, the SD is at a high level because the simple model cannot handle these data. The error area is narrowed with more complicated models. Largely, the SDs of DT models are similar to those of MLR models.
(a) Average training and testing performance of DT models

(b) Regression decision tree

Fig. 2 The performance of DT models and the selected decision tree

For DT-2, the DT model with the closest training and testing $R^2$ to the average training and testing $R^2$ is selected among 50 trials, in order to explore the tree structure. The selected decision tree appeared on the 19th trial, shown in Fig. 2(b). It has a training $R^2$ of 0.854 and a testing $R^2$ of 0.764. Other DT-2 models that have similar $R^2$ present the same tree structure.
with only the regression value at the leaf nodes different. Thus, it is reasonable to perceive the regression process by this model.

### 5.3 Grey model (GM)

The GRA results show the FS (0.898), CO (0.865), and FC (0.863) have almost the same grey relational grades. PO (0.767) is the fourth input factor, followed by GC (0.590).

With the ranked input factors from GRA, 10 grey models were built based on different input factors. The training and testing results are shown in Fig. 3. For GM(1,$n$), the best fitting model is GM(1,3), with a training $R^2$ of 0.977 and a testing $R^2$ of 0.959, involving FS and CO. With the number of factors increasing, the model performance is not stable. For GMC(1,$n$), the grey models perform more steadily as more input factors are fed into the models. The best GMC model is GMC(1,6), with a training $R^2$ of 0.991 and a testing $R^2$ of 0.977. Moreover, the error area also contains important information. Most of the GM(1,$n$) models have high SDs, indicating these models are unstable. However, the case of GMC(1,$n$) is different. For GMC(1,5) and GMC(1,6), the widths of the training error area almost shorten to perfectly zero, and the testing SDs are also lowered to an acceptable level.
Among 50 trials of GMC(1,6), the model with the closest training and testing $R^2$ to the aforementioned average $R^2$ was found in the 18th trial, with a training $R^2$ of 0.993 and a testing $R^2$ of 0.967. In Eq. (4), the model parameter is identified: $a = -0.0694$, $b = [-0.0461, -0.3489, 0.4774, -0.1028, 17.6166]$, $u = -2079.5973$. With these model parameters, the selected model is determined. This model has great fitting ability but poor interpretive ability.

### 5.4 Artificial neural network (ANN)

ANN modeling needs a dataset for validation, which can be regarded as a training process. In each training epoch, the validation data measures the model’s generalization ability. The training process is terminated when the generalization no longer improves. The previous 80% of data was divided into 70% for training and 10% for validation. Six ANN models were trained, and the results are shown in Fig. 4. The training $R^2$ goes up with the number of neurons in the hidden layer growing. As shown in Fig. 4, the testing $R^2$ first increases and then decreases. The increase in testing $R^2$ is due to the enhanced fitting ability as the underfitting model becomes more complicated. The decrease in the testing $R^2$ means poor generalization to test data and unreliable predictive performance.
Fig. 4 Average training and testing performance of ANN models

In this study, the best-performing model is ANN-15, with 15 neurons in the hidden layer. It has a training $R^2$ of 0.930 and a testing $R^2$ of 0.914. Both underfitting and overfitting models have larger SDs. The best-performing model is relatively stable in terms of prediction performance. Among 50 trials of ANN-15, the model with the closest training and testing $R^2$ to the aforementioned average $R^2$ occurred in the 35th trial. This model has a training $R^2$ of 0.925 and a testing $R^2$ of 0.918. However, this model has many nested sub-structures, making it difficult to trace the influence of each input factor. The meaning of each parameter in neurons is elusive due to the high complexity of the model architecture.

5.5 Summary of models

The best-performing models for each modeling method are PCA-MLR-5, DT-2, GMC(1,6), and ANN-15. The predicted results are shown in Fig. 5, with all the points evenly distributed on both sides of the 45-degree line. The GMC(1,6) has the best performance with the highest training and testing $R^2$, followed by ANN-15. These two models are well known for their strong fitting ability. The DT-2 and PCA-MLR-5 models rank third and fourth, respectively. Both of these two models have strong interpretability. The MLR model can tell the major predictors. However, an MLR model can only depict the linear part of a system, which is why it cannot achieve high accuracy. The DT model presents clear logical rules in a tree-based manner, understandable to a person without knowledge of mathematics and statistics. To some extent, the MLR and DT models sacrifice their ability to fit but gain stronger interpretability as compensation. The four best-performing models were also adopted to
forecast C&D waste generation in GBA cities in 2018. The forecast results show that 11 cities in the GBA produced about 364 million m$^3$ of C&D waste in 2018. The details about the predicted and forecast results of the four best-performing models can be found in the Supplementary Materials.

Fig. 5 The predicted results of the four best-performing models

6. Discussion

6.1 Methodological contributions

Numerous algorithms and models are emerging for estimating waste generation. In this study, four popular and representative ML models, namely MLR, GM, ANN, and DT, were selected and built to estimate C&D waste generation in the GBA, China. Compared with the relevant studies summarized in Table 2, all models in this study are able to deliver acceptable results, implying that the selected factors can explain most variations in C&D waste generation in a region. GM has the highest $R^2$. GM is a series of differential equations by nature. The meanings of parameters in such equations are sometimes overly abstruse. Existing studies tend to report its applications in forecasting solid waste and emphasize its high accuracy. Little literature has explained the meaning of the parameters. Likewise, the results recorded in this study do not provide much explanatory information other than accurate predictive value.

ANN, as a powerful ML technique, has also been widely adopted in estimating solid waste generation. ANN is capable of modeling arbitrarily complex nonlinear relations between
inputs and outputs, as long as there are enough neurons in the hidden layer. More neurons in the hidden layer make the model entail more model parameters and lead to a huge and complex architecture. These complicated models can also fall into the overfitting trap. In this study, the best-performing ANN models had almost equal performance. Therefore, overfitting is less an issue in this study. Nevertheless, there is no guarantee that this model will perform well on other data sets. Moreover, it is hard to decipher the mechanism behind the models to transfer inputs to outputs. Like GM, the results from ANN are just the predictive value of C&D waste generation without explaining why these values are obtained.

Compared with nonlinear models as mentioned above, an apparent benefit of linear models is that the model parameters have their practical meanings. In this study, the MLR model illustrates that factors having a great impact include CO and GC, which may demonstrate the level of construction activity and construction waste management, respectively.

DT provides $R^2$ results of more than 0.75 for both training and testing, which is within the acceptable range. Two factors, namely PO and GC, were used in building the decision tree. Although there is no denying that these two factors do matter, some of the information (e.g., different levels of construction activity) may be neglected. The DT model only produces six predictive values, which may have discrepancies with reality. Nevertheless, it still can give a rough but reliable estimation for reference.

Some of the ML models can achieve high accuracy by developing very intricate models with strong fitting ability. Such models do have significance in research, but may experience the problems of overfitting in practice. One solution is to train the model with more data. It is obviously not feasible in forecasting C&D waste generation in regions with poor statistics in presence. However, encouragingly, some well-managed cities have started collecting data about C&D waste generation in recent years. Another solution is to avoid complex models. When it is impossible to incorporate all influencing factors to produce a deterministic model, there is a wisdom to “think less”, especially in the case of insufficient data. A simple model may be more robust, reliable and interpretative. Therefore, this study calls for paying the same attention to simple and indicative models as complex and accurate models.

To summarize, each ML model has its own strength and weakness (see Table 3). Among those considered, GM and ANN results are more accurate, while MLR and DT contain more understandable information. The better solution is to look at them more comprehensively. It is vital to not only try those models with high accuracy, but also employ interpretative models when estimating C&D waste generation.
Table 3 The strength and weakness of prediction models in this study

<table>
<thead>
<tr>
<th>Prediction model</th>
<th>Strength</th>
<th>Weakness</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multiple linear regression (MLR)</td>
<td>Strong interpretability; Simple implementation with lower time complexity.</td>
<td>Inability to describe the nonlinear part of datasets.</td>
</tr>
<tr>
<td>Decision tree (DT)</td>
<td>Strong interpretability; Ability to model the nonlinear relationship.</td>
<td>Prone to fall into the local optima; Prone to overfitting.</td>
</tr>
<tr>
<td>Grey model (GM)</td>
<td>Possible to produce accurate prediction results; Only require small datasets.</td>
<td>Poor interpretability.</td>
</tr>
<tr>
<td>Artificial neural network (ANN)</td>
<td>Strong prediction performance; Ability to modeling various complex nonlinear relationships.</td>
<td>Poor interpretability; Prone to fall into the local optima; Prone to overfitting.</td>
</tr>
</tbody>
</table>

6.2 Practical implications

The findings of this study mainly have several practical implications for researchers, policymakers, or environmental protection groups. Firstly, the information, e.g., the estimated C&D waste generation in a region, can be used for examining urban metabolism with a view to developing a circular economy. Urban metabolism is widely applied to describe how material, food, energy, and water consumed by urban as an eco-system to support its growth and reproduce, and consequently generate products and by-products (e.g., GHG, pollutants, and waste) (Kennedy et al., 2007; Wolman, 1965). The amount of C&D waste generation is an indispensable parameter to understand the urban, in particular industrial eco-system metabolism (Zhang et al., 2018). It is also a useful indicator to understand the efficiency of a circular economy system (MacArthur, 2013), which aims to turn some of the waste materials into more circular uses.

Secondly, the estimated C&D waste generation amount can be used for a series of evidence-based policy-making. For example, it can be used for planning the waste management capacity in a region, e.g., the landfill space, the existing and expected 3R capacities. Planners often face the problem of a lack of data when performing this practice. Based on the magnitude of the problem and waste management capacity, policymakers can further make proper arrangements on incentives for recyclers and penalties for polluters. The incentives, including subsidies, tax deduction, and low-cost land usage, have been adopted previously to help recyclers bolster profitability (Bao et al., 2019). Penalties, such as CWDCS in Hong Kong, could impel polluters to minimize C&D waste generation (Lu & Tam, 2013). The information can also be used for inter-regional coordination. For example, the boundary of an urban metabolism system is extended to several regions owing to the globalization of construction resources. Under this circumstance, policymakers are exploring extended producer responsibility (Xu et al., 2021) or cross-jurisdiction waste material sharing (Lu et al., 2020). The reliable estimation of waste generation in this study will provide one of the most important information pieces for these policy-making efforts.
Last but not least, the amount of waste generation can be used for a series of public engagement activities. For example, by presenting the capacity of recycling and landfill and the generation of C&D waste, the urgency of the problem can be better sensed by the general public. As a result, it may better urge stakeholders to avoid the Not-In-My-Back-Yard mindset (Bao et al., 2021), and to more consciously engage in pursuing a circular economy (Ruiz et al., 2020). Performed periodically, this estimate will provide a longitudinal data set, which shows the trend of the CWM performance, hopefully, will allow people to achieve a virtual circle between built environment development and natural environment protection.

7. Conclusion

Data on waste generation at a regional level is of paramount importance to devising proper waste management strategies, but many regions, in particular emerging ones, lack reliable data of this kind. Focusing on the Greater Bay Area (GBA) in China, one of the most economically dynamic areas in the world, this study estimates construction waste generation using limited, publicly available data and proper data analytics. The five factors of population, GDP per capita, total construction output, floor space of newly started buildings, and floor space of buildings completed were adopted. The data analysis results show that these factors can explain most of the variations of C&D waste generation and the coefficients of determination ($R^2$) reach the level of 0.75 or above. Construction waste generation in individual regions of the GBA can be estimated. These are useful data for developing waste management strategies, for example, monitoring the urban metabolism of input (e.g., materials, energy) and output (e.g., waste), quantifying carbon emission and impacts on climate changes, planning waste management facilities (e.g., recycling plants or landfills), promoting cross-jurisdictional waste material sharing, and so on. This method of estimating construction waste is a useful reference for other regions considering their own dilemma over development and environment.

This study also contributes to the methodology for estimating waste generation. Four types of popular and powerful ML models, namely multiple linear regression (MLR), decision tree (DT), Grey models (GM), and artificial neural network (ANN) were selected and compared by their strengths and weaknesses. The four models all achieved high accurate predictions of waste generation, as evidenced in the high $R^2$. Amongst them, GM and ANN have higher prediction accuracy but are more like “black boxes”, not readily accessible to readers. One should also avoid overfitting issues when using the models. In contrast, MLR and DT have slightly lower prediction accuracy but allow more information understandable to readers about the predicting mechanism.

This study has its share of limitations. Firstly, it is based on limited data points, regardless of the best efforts paid to data collection. More model calibration works are expected in the
future using other methodological approaches (e.g., Geographic Information System) when more data is available. Secondly, although it is legitimate to use data-rich regions to extrapolate data-scarce ones, individual features of each region (e.g., Hong Kong’s long leading role in waste management; Shenzhen’s ambitious zero waste initiative) are yet to be considered in the estimation. Thirdly, estimating future waste generation based on present data is inherently inaccurate. Hence, researchers should adopt a dynamic perspective, monitor the modeling effects, and adjust if necessary. Finally, the biggest motivation of such estimation works is to apply the results in real life. Future studies are encouraged to implement this study in the GBA and receive further verification.

Acknowledgment
This research is supported by the Strategic Public Policy Research Funding Schemes (Project Number: S2018.A8.010.18S) from the Hong Kong SAR Government.

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