BSS-Indoor: Volumetric wall reconstruction using Building Section Skeleton

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Wu, Y., Meng, S., & Xue, F. (2024). BSS-Indoor: Volumetric wall reconstruction using Building Section Skeleton. *Proceedings of the 29th International Symposium on Advancement of Construction Management and Real Estate (CRIOCM2024)*, Springer, in press.

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- Abstract. Building Information Modeling (BIM) has become well recognized and increasingly mandated
- ⁶ in the building sector, where Scan-to-BIM automation shows great potential for BIM users. For the 'last
- 7 mile' or 'last step' of automatic Scan-to-BIM, parametric reconstruction, existing methods focus on
- ⁸ surface reconstruction. However, BIM practitioners have to handle architectural elements as volumetric
- ⁹ instances rather than connected surfaces. This paper proposes a volumetric reconstruction method called
- ¹⁰ BSS-Indoor. The method is based on a novel Building Section Skeleton (BSS) theory which pairs the
- parallel and symmetric facades of the building exterior. By adapting BSS from building exteriors to
- ¹² interiors, BSS-Indoor reconstructs internal walls as BSS segments. Our method simultaneously locates
- ¹³ walls and estimates their thicknesses, addressing common issues in existing solutions, such as fragmented
- ¹⁴ long walls and merged adjacent walls. Preliminary experiments on a subset of the CV4AEC (3D) dataset
- ¹⁵ demonstrate the effectiveness and potential of BSS-Indoor in reconstructing volumetric walls.

¹⁶ Keywords: Scan-to-BIM; Volumetric wall reconstruction; Point cloud processing

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17 **1 Introduction**

The Building Information Modeling (BIM) has become significantly important throughout a building's 18 entire lifespan, covering all phases from initial design to eventual demolition [1]. To streamline the 19 building sector with BIM, automating the creation of BIMs is extremely crucial [2]. Scan-to-BIM, a 20 popular task that converts 3D scans captured by laser scanners or photogrammetry, shows great potential 21 in the creation and uses of as-is BIM [3]. A typical Scan-to-BIM workflow involves four steps: scanning, 22 scan registration, semantic segmentation, and parametric reconstruction. In recent years, solutions and 23 datasets for registration and semantic segmentation of building interiors have rapidly evolving, which 24 significantly boosted the Scan-to-BIM popularity [4]. However, the parametric reconstruction, which is 25 the 'last mile' or 'last step' of the Scan-to-BIM pipeline, does not yet fulfill the actual requirements of 26 BIM practitioners in the industry [5]. 27

Existing methods for reconstructing building interiors focus on surface reconstruction instead of vol-28 umetric modeling. These methods reconstruct the surfaces of architectural elements, i.e., walls, floors, 29 and ceilings, into lightweight meshes [6, 7]. Simultaneously, rooms and their closed boundaries are 30 extracted [8, 9]. The resulting surface models or floorplans satisfy the requirements of indoor naviga-31 tion [10] and fit the native geometric representation of CityGML for City Information Modeling [6]. 32 However, BIM practitioners in the building sector pay more attention on the individual instances of ar-33 chitectural elements [5]. Walls and slabs are preferably modeled as volumetric instances enriched with 34 joints and details inside the surfaces rather than separated facets that bound different rooms. 35

Volumetric reconstruction of architectural elements essentially involves locating the volume, outlines 36 the volumetric shape and/or estimates the dimensions of the identified volume. For walls and slabs, 37 thickness should be estimated. Meanwhile, walls are usually simplified as cuboids. Volumetric walls can 38 be reconstructed by clustering the wall points produced by semantic segmentation and then estimating 39 the bounding box of each cluster [4]. To achieve a higher reconstruction fitness to the scans, optimiza-40 tion models were formulated to finetune the locations and dimensions of wall boxes [11]. Moreover, 41 wall thickness can also be predicted by deep learning after projected the point clouds onto horizontal 42 planes [5]. However, as the height information is missing after the projection, the method reconstructs 43 floorplans only. A common aspect among these solutions is that they separate the volume localization and 44 dimension estimation processes. As a result, long walls are prone to being cut into pieces and adjacent 45 walls with different dimensions are prone to being merged into one wall. 46

In this paper, we propose a volumetric reconstruction method for walls based on the Building Section 47 Skeleton (BSS) [12]. Our method aims to locate and estimate the thickness of walls simultaneously. BSS 48 is a shape skeleton defined to adapt the morphological characteristics of building exterior boundaries. 49 Each BSS segment corresponds to a pair of parallel vertical planes representing facades or a pair of 50 symmetric incline planes representing roofs. A BSS segment is parameterized with the radius and forms 51 a polyhedron, which is a similar concept of volume thickness. This study transfers the BSS for building 52 exteriors to interiors. Each internal walls are reconstructed as a BSS segment, while the external walls 53 are detected as the parallel facades that bound buildings. Preliminary experiments on the a subset of the 54 CV4AEC (3D) dataset [13] show that our method, named BSS-Indoor, can effectively reconstruct the 55 volumetric walls. 56

The remainder of this paper will introduce our method BSS-Indoor, report preliminary results, as well as discuss the strengths and future improvement of BSS-Indoor.

⁵⁹ 2 Preliminaries: Building Section Skeleton for wall reconstruction

The fundamental concept of the Building Section Skeleton is to capture the parallel and symmetric planes of buildings, building on the classical concept, shape skeleton, in computer graphics. The identified parallel and symmetric planes can be assembled into 3D volumes which represent the space inside buildings, providing semantic information. These 3D volumes may corresponding to the empty space of building interiors designated for specific functions, such as offices and corridors, or they could also be physical structures, such as walls.

BSS are defined at three levels, i.e., atoms, segments, and the relations between segments. A BSS 66 atom is the center of the sphere inscribed by symmetric points on the exterior or interior surfaces of 67 buildings. If the surfaces are vertical, the radius of the sphere and the normals of the inscribed points 68 are attributes of a BSS atom. If the surfaces are not vertical, the intersection height of the two inscribed 69 directions and the normals of inscribed points serve as the parameters of a BSS atom. When two points 70 lie on a pair of parallel planes, then the corresponding BSS atom is equivalent to the midpoint of these 71 two points. At the second level in the definition of BSS, a segment is a group of BSS atoms distributed 72 on a same plane, forming a region, and sharing same radius or intersection height and normal. Hence, a 73 BSS segment represents the medial plane of a pair of parallel or symmetric planar regions. Furthermore, 74 by sweeping the medial vertical region of a BSS segment, there is a corresponding volume of a BSS seg-75 ment, which represents the empty or physical space of buildings. The relations of BSS segments, which 76 constitute the third level of the BSS definition, refer to their topological relations, including intersections 77 and adjacency. For more details on BSS, please refer to [12]. 78

In the practice application of BSS in Scan-to-BIM, there are two specific designs for wall reconstruc-79 tion. Although a BSS segment could be the medial planar region of both vertical and incline planes which 80 could be parallel and non-parallel, respectively, the planes involved in wall reconstruction are usually par-81 allel. Therefore, we solely use BSS for vertical and parallel planes. Moreover, different mechanisms are 82 employed reconstructing interior and exterior walls. As a BSS segment represents the medial plane of 83 a pair of parallel or symmetric planes, the use of BSS assumes the presence of dual planes to bound a 84 space. However, the scanned point clouds for BIM reconstruction may not always include the facades 85 of buildings, leaving only one single plane for an exterior wall. To reconstruct both interior and exterior 86 walls, our method captures dual wall surfaces as close as possible to each other for reconstructing BSS 87 segments for interior walls, and as far apart as possible for reconstructing the interior spaces of buildings. 88 Subsequently, we use the boundaries of the interior spaces to supplement the exterior walls. 89

90 **3 Method**

91 3.1 Overview

Fig. 1 shows an overview of our method. BSS-Indoor takes the segmented point clouds of architectural
elements as inputs and outputs the volumetric walls. Plane detection is performed first to group points as
planar primitives. Then, the method clusters the primitives in terms of their normals. In the case shown
in Fig. 1, two orthogonal orientations are clustered. After that, two stages, one for proposing, the other
for refining, are implemented to reconstruct the walls of each orientations.

Stage 1 locates the possible walls and outlines their vertical planar boundaries as the initial BSS
 segments. This stage pairs the parallel planar primitives of each orientation whose distances between
 each other are close or far apart enough in terms of given thresholds. After pairing, the proposed method



Figure 1: Overview of BSS-Indoor.

segments the common regions coarsely of each paired regions in an ascending order for close ones and descending order for far away ones. Note that the common region is the vertical medial region of the paired planes. However, as shown in Fig.1, the initial BSS segments have irregular boundaries. There are also topological errors including intersections and gaps between different BSS segments.

Therefore, Stage 2 further refines the BSS segments by aligning the BSS segments of different orientations to smooth the boundaries and remove the intersections and gaps. The aligning procedure projects the vertical regions of a BSS segment onto a vertical plane. The method then triangulates the projected extent. Triangles in the extent are labeled as inside or outside the BSS segment. Refining the boundary of a BSS segments now can be conducted by flipping the inside/outside labels of the triangles. An integer programming model is formulated to optimize the flipping for a smooth and topologically correct boundary of each BSS segment.

After the two stages, internal walls are reconstructed from the BSS segments formed by close paired planes, while external walls are from BSS segments composed by far apart parallel planes. The method extrudes the vertical region of a BSS segment horizontally by the radius of a BSS segment for interior walls or a standard thickness for exterior walls.

115 3.2 Stage 1: Pairing and Segmentation

In Stage 1, parallel planes within each cluster are paired, and the common regions of the paired planes are segmented for each orientation individually.

Planes within a cluster that are either closer or farther than given thresholds are filtered as potential pairs. Then, the method sorts the pairs with small distances in an ascending order for reconstructing interior walls, while pairs with large distances in descending order for exterior walls. The segmentation of the common regions for interior and exterior walls are performed individually according to their respective orders. Although a plane can be paired with multiple planes, a region of the plane can only be segmented once and paired with one of its pairing candidates. Therefore, within a single orientation cluster, BSS segments and their corresponding volumes cannot intersect with each other. By design, paired planes with closer distances are segmented first for interior walls; whereas farther paired planes are prioritized
 for exterior walls.

The segmentation of common regions are based on the Boolean operations of polygons. Our method projects the points of each plane onto a vertical plane and then polygonizes the projected regions by calculating their 2D Alpha shapes. When segmenting the common region for a pair of planes (A, B), the two polygons of each plane are separated into three parts: $A \cap B$, $A \setminus B$, and $B \setminus A$. The region of $A \cap B$ is segmented out as one of the initial BSS segment. The regions of $A \setminus B$ and $B \setminus A$ are retained for the subsequent segmentation with the remaining paired planes of A and B, respectively.

After segmenting the region of a BSS segment, our method extrudes the vertical region of a BSS segment horizontally in both orientations by its radius to form a 3D polyhedron, representing the initial interior walls and indoor spaces (presented in the two sub-figures on the left-hand side in the second row in Fig. 1).

137 3.3 Stage 2: Alignment

Stage 2 refines the initial BSS segments by aligning those of different orientations. This process includes
 smoothing the boundaries of the BSS segments and eliminating intersections and gaps between them.

The alignment procedure relies on the intersections of BSS segments from various orientations. The 140 method first intersects the medial planes of the initial BSS segments, filtering out intersection lines that 141 are too distant from the segmented regions. Next, for each orientation cluster, our method projects all 142 the segmented common regions from Stage 1, along with the intersection lines, onto the vertical plane 143 orthogonal to the orientation. Constrained triangulation is performed on the projection. The resulting 144 triangles are labeled based on whether they belong to a particular segment or not. Assume there are n145 segments in a cluster; each triangle is labeled with a k-dimensional binary vector. The refinement of 146 initial BSS segments is then transformed into a problem of flipping the labels of these triangles. 147

A binary optimization model is formulated for the label flipping. The Boolean variables indicate 148 whether a label should be flipped, or equivalently, a triangle should be removed from or added to a BSS 149 segment. The smoothing and topology refinement are achieved by controlling the label distinctions of 150 triangles distributed across the intersection lines. Adjacent triangles sharing edges on the intersection 151 lines are prone to be labeled differently; that is, if one belong to a BSS segment, the other should not 152 belong to the same BSS segment. For adjacent triangles whose common edges are not on the intersection 153 lines, the optimization model tends to label the two triangles in a same way, i.e., both either belong to 154 or do not belong to a BSS segment. As a result, the optimization encourages continuity inside a BSS 155 segment and discontinuity along the intersection lines, which drives the boundaries of the BSS segments 156 to align with the intersection lines. Additionally, the refinement should not deviate significantly from the 157 initial BSS segments. Therefore, the optimization model also minimizes the number of label flipping. 158

4 Preliminary experiments

4.1 Data and implementation details

To validate the initial effectiveness of BSS-Indoor, six samples from the training set of the CV4AEC 3D dataset were tested. Note that this dataset was captured by laser scanners. As a result, there are missing points for walls and outliers outside the buildings due to windows. The six samples include two typical scenarios: office and parking. For the following experiments, the point clouds were uniformly sampled 165 at an interval of 2cm.

The semantic point clouds of architectural elements were segmented by PointContrast [14] which 166 were trained on ScanNet [15] and S3DIS [16]. Plane primitives of the semantic point clouds were de-167 tected by RANSAC [17]. We employed K-Means for clustering the plane orientations, where users need 168 to provide the number of clusters k in advance. In Stage 1, the Alpha shape polygonization of the plane 169 primitives was implemented based on GEOS [18]. The hyper-parameter α was set to a range from 1 to 170 3 m. In Stage 2, the constrained triangulation was implemented based on CGAL [19]. The optimization 171 of integer programming was solved by Gurobi [20] with a weight factor provided by users to balance the 172 geometric consistency and the degree of alignment. 173

174 4.2 Evaluation

Results were evaluated by the official 3D evaluation code [21] of CV4AEC's Scan-to-BIM competition.

¹⁷⁶ The evaluation metrics include 3D Intersection-over-Union (IoU) and the matching precision, recall, and

F1-score of the 2D wall segments. Note that the matching of the 2D segments were evaluated at three

different resolutions with matching thresholds of 5, 10, and 20 cm, respectively.

179 4.3 Results

The reconstructed volumetric walls and the evaluation results are presented in Fig. 2 and Tab. 1. The average 3D IoU is 20.4 %, with a range of 7.4 % to 28.7 %. At the 10-cm resolution, the average precision, recall, and F1 scores are 41.4 %, 41.2 %, and 40.6 %. The precision and recall show a good balance. The F1-scores at 10-cm resolution range from 21.2 % to 56.1 %. As shown in Fig. 2, some internal walls and their thicknesses are accurately estimated, as BSS-Indoor captured their dual planes correctly. The external walls were also partially reconstructed. However, there are still some noticeable limitations, particularly for missing walls.

Table 1: Evaluated results of the 6 samples in CV4AEC 3D dataset. #gt, #pred, #m refer to the number of ground truth, prediction (reconstruction), and matched walls, respectively. The matching between 2D wall segments were evaluated with three matching thresholds of 5, 10, and 20 cm.

				thresh: 5 cm					thresh: 10 cm				thresh: 20 cm			
sample	#gt	#pred	3D IoU	#m	prec.	rec.	F1	#m	prec.	rec.	F1	#m	prec.	rec.	F1	
06_B1	496	712	7.4%	68	9.6%	13.7%	11.3%	128	18.0%	25.8%	21.2%	172	24.2%	34.7%	28.5%	
06_F3	976	856	7.5%	169	19.7%	17.3%	18.4%	217	25.4%	22.2%	23.7%	243	28.4%	24.9%	26.5%	
07_F5	904	544	21.0%	198	36.4%	21.9%	27.3%	290	53.3%	32.1%	40.1%	368	67.6%	40.7%	50.8%	
32_F1	528	640	31.3%	214	33.4%	40.5%	36.6%	311	48.6%	58.9%	53.3%	340	53.1%	64.4%	58.2%	
32_F2	656	688	26.3%	249	36.2%	38.0%	37.1%	333	48.4%	50.8%	49.6%	376	54.7%	57.3%	56.0%	
32_F3	688	728	28.7%	301	41.3%	43.8%	42.5%	397	54.5%	57.7%	56.1%	433	59.5%	62.9%	61.2%	
Average	/	/	20.4%	/	29.4%	29.2%	28.9%	/	41.4%	41.2%	40.6%	/	47.9%	47.5%	46.9%	

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The current BSS-Indoor implementation failed to reconstruct some external walls. As shown in Fig .2, such failures are more significant for Samples 06-B1, 06-F3, and 32-F3. This issue occurred because there might be large empty regions on the external walls where there are large windows. As a result, holes could be observed in the original scans, semantic point clouds, and the initial alpha polygons of the plane primitives, making it difficult to reconstruct the external walls.

Significant incompleteness in the semantic point clouds and initial alpha polygons also led to the
 missing internal walls. These failures could be common due to the heavy occlusions caused by clutter
 near the walls.



Figure 2: Results of the 6 samples. The right sub-figure for each case displays the matching between the ground truth (in blue) and reconstruction (in red).

195 Discussion

We believe that BSS-Indoor has significant potential in calling for research interest on the volumes of 3D 196 objects above points and triangles. Our method separates the reconstruction of the dual-plane walls (usu-197 ally internal walls) and single-plane walls (usually external walls), offering higher flexibility in thickness 198 estimation. By distinguishing these two situations, the thickness of a dual-plane wall is calculated as 199 the distance between its paired planes, while the thickness of a single-plane wall can be estimated or as-200 signed by user-specific, average, or standard wall thickness. Furthermore, BSS-Indoor can clearly detect 201 single-plane walls, allowing users to manually review and adjust them if necessary. Importantly, BSS-202 Indoor does not rely on any learning techniques requiring large-scale manual annotations for thickness 203 estimation, which makes it easier for BIM practitioners to adopt our method in the future. 204

There are also a lot more details should be improved for the current BSS-Indoor, including (1) finetuning the parameters of PointContrast on CV4AEC dataset; (2) adjusting the hyper-parameters of plane detection, Alpha shape polygonization, and the optimization for aligning the BSS segments; (3) debugging the current implementation; (4) testing the method on more samples. Addressing these limitations could lead to enhanced performance and more accurate results.

210 6 Conclusion

In this paper, we introduced BSS-Indoor, a novel volumetric reconstruction method for walls based on 211 Building Section Skeleton. Our method successfully adapts BSS for building interiors and simultane-212 ously locates and estimates wall thicknesses. BSS-Indoor differentiates between the reconstruction of 213 dual-plane walls and single-plane walls, enhancing the accuracy and flexibility of wall thickness esti-214 mation. Preliminary experiments on the CV4AEC (3D) dataset show the effectiveness of BSS-Indoor 215 in reconstructing volumetric walls. Although BSS-Indoor demonstrates potential, further refinement is 216 required to meet the standards necessary for real-world Scan-to-BIM practice in the building sector. Fu-217 ture work will focus on improving the implementation and addressing the limitations identified in the 218 preliminary experiments. 219

Acknowledgments

The work described in this paper was supported by the Hong Kong Innovation and Technology Fund (ITF) [grant numbers ITP/004/23LP].

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